Academy of Economic Studies Doctoral School of Finance and Banking

CREDIT SCORING MODELING -A MICRO MACRO APPROACH-

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Topics

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- 2. Objectives
- 3. Literature Review
- 4. Methodology and data input
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1.Motivation

• Classification models in the form of scorecards, use predictor variables (or characteristics) from credit application forms and other sources to yield estimates of the probability of default.

• Banks and financial institutions play an important role in the economy as providers of credit. Beside government supervision and other regulatory conditions, capital requirements limit risks for depositors, and reduce insolvency and systemic risks. Unnecessary capital requirements restrain credit provision needlessly, whereas inadequate capital requirements may lead to undesirable levels of systemic risk.

2.Objectives

- Estimation of probabilities of default ;
- Event Trigger for Retail Credit Risk, financial vs. socio-demographic variables ;
- Including of a macroeconomic indicator at level client;
- Minimizing the loss function for the analyzed models;
- Stressing the client's income due to cutting-off wages for public sector employers.

3.Literature Review

- In 1997, Hand and Henley made a comparison among logistic regression ,neural networks and other techniques and in their paper also present the Information Value criterion of selection variables;
- West(2000) investigates the credit scoring accuracy of five neural network models and compared them with other techniques such as logistic regression, decision trees etc and the results demonstrate that although neural networks have better results logistic regression is a good alternative to them;
- Komorád (2002) investigated credit scoring prediction accuracy and the methods, namely the logistic regression and multi-layer perceptron (MLP) give very similar results, however the logit model seems to perform marginally better;
- Bellotti and Crook (2007) show that survival analysis is competitive for prediction of default in comparison with logistic regression and also they included macroeconomic variables and a cost decision matrix. Malik and Thomas(2008) incorporated both consumer specific ratings and macroeconomic factors in the framework of Cox proportional hazard model.
- Rommer(2005) come to idea that there is no major difference between logit and probit regression models.
- Rauhmeier(2006) analyzed the validation process for probabilities of default and includes also the concept of "rolling window 12 months " and in 2010,Sabato also presents the importance of the model's validation and how back testing is the essential part of this process.

4.Methodology and data input

•Logit Model

$$\log\left(\frac{p_{i}}{1-p_{i}}\right) = w_{0} + w_{1}x_{1} + w_{2}x_{2} + \cdots + w_{p}x_{p} = w \cdot x^{T}$$

•Probit Model

$$N^{-1}(p_i) = w_0 + w_1 x_1 + w_2 x_2 + \cdots + w_p x_p = w \cdot x^T$$

•Neural Networks



4.Methodology and data input

A multilayer perceptron is composed of an input layer of signals, an output layer and a number of layers of neurons between, called hidden layers.

K₁₁

K₁₂

K_{gr}

 $\Sigma | F$

 $\Sigma|F$

 $\Sigma|F|$

 $\Sigma | F$

 $\Sigma|F$

 $\Sigma | F$

w_{rp}



Income

4.Methodology and data input

- The default definition is set according to Basel II (90 days overdue);
- The data base consists of 33,321 observations representing private individuals that have been granted a loan between January 2006 and December 2008;
- Each client has been observed for the first 12 months after the approval so the period of observation is January 2007 –December 2009.
- The realized default rate for portfolio is 14.81%
- Based on year of approval , data have been split up in three sub samples.

Performance Measures

The requirements of the IRB approach is that "the institution shall have a cycle of model validation that includes monitoring of model performance and stability "

| | | Ac | tual |
|--------|-------------------|-----------|-------------------|
| | | Defaulter | Non- Defaulter |
| dicted | Defaulter Non- | А | С |
| Pre | Defaulter | В | D |

$$Sensitivity = \frac{A}{B+A}$$

 $Specificity = \frac{D}{C+D}$

$$AR = \frac{A_R}{A_P}$$
$$AR = 2A - 1$$



Performance Measures

•Brier Score

$$BS = \frac{1}{n} \sum_{n=1}^{n} (p_n^{forecast} - \theta_j)^2 \qquad \theta_j = \begin{cases} 1, \\ 0, \end{cases}$$

if obligor j defaults otherwise

•Spiegelhalter test

$$Z = \frac{BS - E[BS]}{\sqrt{Var[BS]}} \sim N(0,1)$$

$$Var[BS] = \frac{1}{N^2} \sum_{i=1}^{N} (1 - 2p_i^{forecast})^2 \cdot p_i^{forecast} \cdot (1 - p_i^{forecast})$$
$$E[BS] = \frac{1}{N} \sum_{i=1}^{N} p_i^{forecast} \cdot (1 - p_i^{forecast})$$

•Kuiper Score KS = Hit Rate - False Alarm Rate

•Granger-Pesaran Test

$$GP = \frac{\sqrt{NKS}}{\sqrt{\frac{p_f(1-p_f)}{p_a(1-p_a)}}} \sim N(0,1)$$

Indicator of Macroeconomic Vulnerability

• With the advent of the Basel II banking regulation it is just not enough to correctly rank customers according to their default risk but also to have an accurate probability of default for each client as these predicted values are used to determine the minimum capital requirement for the portfolio of the retail sector.

•In order to incorporate the changes in economic conditions and to observe the modifications of the quality of the portfolio, variables that catch up the macroeconomic vulnerabilities have been introduced in model.

$IMV_G = \Delta\% UR - \Delta\% NS + \Delta\% IR - \Delta\% IPI + \Delta ER - \Delta\% BET + \Delta\% CPI$

 $IMV_{client} = IMV_G \cdot DTI \cdot Spread$

UR-unemployment rate NS=net average salary IR-reference interest rate IPI=index of industrial production ER=exchange rate BET=Stock Market Index CPI=consumer price index.

 $DTI = \frac{Monthly Payment}{Income - Expenses}$

Spread = Interest Rate – Benchmark Rate

•Stepwise selection-it is starting with a forward selection and then continues with a backward selection in this way a variable could enter and could be removed from the model several times until no further effect can be added to the model or if the effect just enter into the model is the only effect removed in the subsequent backward elimination

•Information Value

$$WOE_{c} = \ln \frac{\% Non - defaulters}{\% Defaulters})$$
$$IV(c) = (\% Non - defaulters - \% Defaulters) * WOE_{c}$$

Information Value =
$$\sum_{i=1}^{k} IV(k)$$

Variable Selection

| | Information Value | | | | | |
|----------------|-------------------|---------|---------|--|--|--|
| Variable | 2006 | 2007 | 2008 | | | |
| AGE | 0.39398 | 0.47938 | 0.44900 | | | |
| BANK_R | 0.24589 | 0.00696 | 0.05127 | | | |
| CCY | 0.01337 | 0.02158 | 0.00689 | | | |
| COUNTY_ID | 0.00014 | 0.00124 | 0.01049 | | | |
| EDUCATION | 1.06506 | 0.22236 | 0.20623 | | | |
| EXPENSES | 0.78089 | 0.62239 | 0.33262 | | | |
| INCOME | 0.87698 | 0.27902 | 0.13908 | | | |
| INDUSTRY | 0.39440 | 0.49011 | 0.16557 | | | |
| INTEREST_RATE | 0.31112 | 0.16148 | 0.12133 | | | |
| LOAN_VALUE | 0.67563 | 0.26445 | 0.25619 | | | |
| MARITAL_STATUS | 0.52518 | 0.33669 | 0.52125 | | | |
| PAYMENT | 0.59730 | 0.31969 | 0.11234 | | | |
| PHONE_ID | 0.03745 | 0.00665 | 0.04046 | | | |
| PRODUCT_ID | 0.13533 | 0.17437 | 0.09027 | | | |
| PROFESSION | 0.39685 | 0.07986 | 0.01145 | | | |
| REPAYMENT | 1.18685 | 1.49617 | 1.15581 | | | |
| RESIDENCE | 0.87919 | 0.37306 | 0.72286 | | | |
| SENIORITY | 0.17727 | 0.66712 | 0.45028 | | | |
| SEX | 0.00116 | 0.00792 | 0.00299 | | | |
| TERM | 0.44065 | 0.18200 | 0.26365 | | | |

*The red colour is for values < 0.1, yellow is for values between 0.1 and 0.2 and green otherwise

5.Empirical Results: A multi-year analysis

| 2007 Neural Networks | Tanh | Logistic |
|---------------------------------------|------------|------------|
| | | |
| Train: Akaike's Information Criterion | 4121.68000 | 3953.43000 |
| | | |
| Train: Schwarz's Bayesian Criterion | 4992.89000 | 4824.64000 |
| Train: Average Error Function | 0.19598 | 0.18748 |
| Train: Error Function | 3879.68000 | 3711.43000 |
| Train: Misclassification Rate | 0.07234 | 0.07254 |
| Train: Number of Wrong | | |
| Classifications | 716.00000 | 718.00000 |
| Valid: Average Error Function | 0.21115 | 0.20798 |
| Valid: Error Function | 1194.24000 | 1176.34000 |
| Valid: Mean Squared Error | 0.05944 | 0.05800 |
| Valid: Misclassification Rate | 0.07284 | 0.07178 |
| Valid: Number of Wrong | | |
| Classifications | 206 | 203 |
| Test: Average Error Function | 0.20589 | 0.19242 |
| Test: Error Function | 582.25500 | 544.16500 |
| Test: Mean of Squared Error | 0.05774 | 0.05252 |
| Test: Misclassification Rate | 0.07497 | 0.07143 |
| Test: Number of Wrong | | |
| Classifications | 106 | 101 |

| 2006 | Analys | sis of Maxim | um Likeliho | ood Estimates Lo | ogit |
|---------------|--------|--------------|--------------------|---------------------|---------------|
| Parameter | DF | Estimate | Standar d Error | Wald Chi- Square | Pr > ChiSq |
| Intercept | 1 | -3.0700 | 1.6965 | 3.2700 | 0.0704 |
| Expenses | 1 | 0.0066 | 0.0008 | 66.9300 | <.0001 |
| Income | 1 | -0.0024 | 0.0004 | 36.4400 | <.0001 |
| Interest_rate | 1 | 0.1465 | 0.0568 | 6.6500 | 0.0099 |
| Loan_Value | 1 | 0.0000 | 0.0000 | 6.3200 | 0.0119 |
| Payment | 1 | 0.0030 | 0.0006 | 24.4200 | <.0001 |

| 2008 | Analysis | Analysis of Maximum Likelihood Estimates Probit(1) | | | | | |
|---------------|----------|--|----------|------------|------------|--|--|
| Parameter | DF | Estimate | Standard | Wald | Pr > ChiSq | | |
| | | | Error | Chi-Square | | | |
| Intercept | 1 | -2.3134 | 0.4657 | 24.6800 | <.0001 | | |
| Age | 1 | -0.0072 | 0.0030 | 5.7500 | 0.0165 | | |
| Expenses | 1 | 0.0006 | 0.0000 | 198.3700 | <.0001 | | |
| Income | 1 | -0.0002 | 0.0000 | 269.6700 | <.0001 | | |
| Interest_rate | 1 | 0.1963 | 0.0255 | 59.4200 | <.0001 | | |
| loan_value | 1 | 2.52E-06 | 6.91E-07 | 13.2800 | 0.0003 | | |
| Payment | 1 | 0.0002 | 0.0001 | 5.5000 | 0.0190 | | |

2008-Performance



| 2008 | 008 Confusion Matrix | | | | | | | Good | lness of | Fit | | |
|----------|----------------------|------|-------|-----|------------|-------------|-------------|----------|----------|---------|--------|-------------|
| | | | | | | | | Misclass | | | | |
| Model | Sample | TN | FN | TP | FP | Sensitivity | Specificity | Rate | KS | AUROC . | AR | Brier Score |
| Logit1 | test | 1200 |) 104 | 148 | 4 9 | 0.5873 | 0.9608 | 0.1019 | 0.6480 | 0.8956 | 0.7913 | 0.0785 |
| Logit 2 | test | 1196 | 5 102 | 150 | 53 | 0.5952 | 0.9576 | 0.1033 | 0.6427 | 0.8936 | 0.7872 | 0.0790 |
| Probit 1 | test | 1204 | l 109 | 143 | 45 | 0.5675 | 0.9640 | 0.1026 | 0.6439 | 0.8961 | 0.7921 | 0.0794 |
| Probit2 | test | 1204 | F 109 | 143 | 45 | 0.5675 | 0.9640 | 0.1026 | 0.6316 | 0.8935 | 0.7870 | 0.0798 |
| NN1 | test | 1212 | 2 102 | 150 |) 37 | 0.5952 | 0.9704 | 0.0926 | 0.6279 | 0.8957 | 0.7914 | 0.0763 |
| NN2 | test | 1199 |) 95 | 157 | 5 0 | 0.6230 | 0.9600 | 0.0966 | 0.6499 | 0.9104 | 0.8208 | 0.0754 |

Out of sample -out of time



One important aspect, when validate a model is that the performance should be also tested on different sample on a different scale of time;

- •2006 *~>* 2007
- •2007 → 2008

| | | (| Confusio | on Matri | X | | | Goodn | ess of Fit | | | |
|-----------|--------|------|----------|----------|----|-------------|-------------|----------|------------|--------|--------|--------|
| | | | | | | | | Misclass | | | | |
| Model | Sample | TN | FN | TP | FP | Sensitivity | Specificity | Rate | KS | AUROC | AR | Brier |
| | | | | | | | | | | | | Score |
| NN2_2008 | test | 1199 | 95 | 157 | 50 | 0.6230 | 0.9600 | 0.0966 | 0.6499 | 0.9104 | 0.8208 | 0.0754 |
| NN2_07_08 | test | 1230 | 162 | 90 | 19 | 0.3571 | 0.9848 | 0.1206 | 0.5679 | 0.8550 | 0.7100 | 0.0978 |
| NN2_2007 | test | 1203 | 74 | 110 | 27 | 0.5978 | 0.9780 | 0.0714 | 0.7415 | 0.9290 | 0.8580 | 0.0525 |
| NN2_06_07 | test | 1180 | 134 | 50 | 50 | 0.2717 | 0.9593 | 0.1301 | 0.4618 | 0.7945 | 0.5891 | 0.1096 |

Portfolio Analysis

• Portfolio results pointed out that the model with minimum prediction error is the neural network with logistic function

| An | alysis o | of Maximum I | Likelihood F | stimates-Logit | : (1) | | |
|---------------|----------|--------------|--------------|----------------|------------|--------|------|
| Parameter | DF | Estimate | Standard | Wald | Pr > ChiSq | Pa | ara |
| | | | Error | Chi-Square | | | |
| Intercept | 1 | -3.2254 | 1.3597 | 5.63 | 0.0177 | Interc | ep |
| Age | 1 | -0.015 | 0.00418 | 12.94 | 0.0003 | Age | |
| Expenses | 1 | 0.00201 | 7.4E-05 | 744.3 | <.0001 | Expe | nse |
| Income | 1 | -0.001 | 3.8E-05 | 684.55 | <.0001 | Incon | ne |
| Interest_rate | 1 | 0.0697 | 0.0272 | 6.58 | 0.0103 | Intere | est_ |
| loan_value | 1 | -5.36E-06 | 8.55E-07 | 39.31 | <.0001 | loan_ | val |
| Payment | 1 | 0.00317 | 0.00014 | 490.89 | <.0001 | Payme | ent |

| Analysis of Maximum Likelihood Estimates-Probit (1) | | | | | | | |
|---|----|-----------|----------|-----------|------------|--|--|
| Parameter | DF | Estimate | Standard | Wald Chi- | Pr > ChiSq | | |
| | | | Error | Square | | | |
| Intercept | 1 | -1.9537 | 0.7119 | 7.53 | 0.0061 | | |
| Age | 1 | -0.00726 | 0.00216 | 11.3 | 0.0008 | | |
| Expenses | 1 | 0.000876 | 3.1E-05 | 808.89 | <.0001 | | |
| Income | 1 | -0.00044 | 1.7E-05 | 718.17 | <.0001 | | |
| nterest_rate | 1 | 0.0415 | 0.0144 | 8.32 | 0.0039 | | |
| oan_value | 1 | -2.71E-06 | 4.28E-07 | 40.11 | <.0001 | | |
| Payment | 1 | 0.00148 | 6.8E-05 | 473.58 | <.0001 | | |

| Analy | Analysis of Maximum Likelihood Estimates-Logit (2) | | | | |
|---------------|--|-----------|-------------------|---------------------|------------|
| Parameter | DF | Estimate | Standard Error | Wald Chi- Square | Pr > ChiSc |
| Intercept | 1 | -1.8361 | 1.3083 | 1.97 | 0.1605 |
| Age | 1 | -0.0152 | 0.00415 | 13.46 | 0.0002 |
| Expenses | 1 | 0.002 | 0.000073 | 748.71 | <.0001 |
| Income | 1 | -0.00099 | 0.000038 | 694.92 | <.0001 |
| Interest_rate | 1 | -0.0287 | 0.0176 | 2.66 | 0.1027 |
| loan_value | 1 | -2.49E-06 | 1.05E-06 | 5.66 | 0.0173 |
| Payment | 1 | 0.00275 | 0.000166 | 276.42 | <.0001 |
| Term | 1 | -0.00006 | 0.000015 | 16.08 | <.0001 |

| Analysi | Analysis of Maximum Likelihood Estimates-Probit (2) | | | | | | |
|---------------|---|------------|-----------|------------|------------|--|--|
| Parameter | DF | Estimate | Standard | Wald | Pr > ChiSq | | |
| | | | Error | Chi-Square | | | |
| Intercept | 1 | -1.2039000 | 0.6881000 | 3.06 | 0.0802 | | |
| Age | 1 | -0.0074700 | 0.0021500 | 12.03 | 0.0005 | | |
| Expenses | 1 | 0.0008770 | 0.0000310 | 818.61 | <.0001 | | |
| Income | 1 | -0.0004500 | 0.0000160 | 734.89 | <.0001 | | |
| Interest_rate | 1 | -0.0142000 | 0.0093800 | 2.29 | 0.1298 | | |
| oan_value | 1 | -0.0000014 | 0.0000005 | 7.13 | 0.0076 | | |
| Payment | 1 | 0.0013000 | 0.0000800 | 264.94 | <.0001 | | |
| Геrт | 1 | -0.0000300 | 0.0000079 | 15.29 | <.0001 | | |

Portfolio Analysis

| Neural Networks | Tanh | Logit |
|--|-----------|----------|
| Train: Akaike's Information Criterion | 10510.42 | 10046.78 |
| Train: Schwarz's Bayesian Criterion | 11678.73 | 11215.09 |
| Train: Average Error Function | 0.21909 | 0.20915 |
| Train: Error Function | 10220.420 | 9756.780 |
| Train: Misclassification Rate | 0.07893 | 0.07631 |
| Train: Number of Wrong Classifications | 1841 | 1780 |
| Valid: Average Error Function | 0.22910 | 0.22547 |
| Valid: Error Function | 3053.480 | 3005.10 |
| Valid: Mean Squared Error | 0.06530 | 0.06478 |
| Valid: Misclassification Rate | 0.08178 | 0.08373 |
| Valid: Number of Wrong Classifications | 545 | 558 |
| Test: Average Error Function | 0.23237 | 0.23123 |
| Test: Error Function | 1548.52 | 1540.89 |
| Test: Mean of Squared Error | 0.06500 | 0.06497 |
| Test: Misclassification Rate | 0.07743 | 0.08103 |
| Test: Number of Wrong Classifications | 258 | 270 |



| Benchmark Study(Accuracy ratio) | Logit | Probit | NN |
|---------------------------------|-------------|--------|-------------|
| Baesens (2005) | 68.60-78.24 | | 66.93-78.58 |
| Galindo and Tamayo (2000) | | 84.87 | 89.00 |
| West(2000) | 76.30-87.25 | | 74.60-87.14 |
| Martens(2007) | 85.7-96.4 | | |

| | | С | onfusio | n Matr | ix | | Goodness of Fit | | | | | |
|----------|--------|------|---------|--------|----|-------------|-----------------|----------|--------|--------|--------|----------------|
| Model | Sample | TN | FN | ТР | FP | Sensitivity | Specificity | Misclass | KS | AUROC | AR | Brier Score |
| Logit1 | test | 2755 | 224 | 295 | 58 | 0.5684 | 0.9794 | 0.0846 | 0.6739 | 0.9042 | 0.8084 | 0.0694 |
| Logit 2 | test | 2751 | 229 | 290 | 62 | 0.5588 | 0.9780 | 0.0873 | 0.6608 | 0.9034 | 0.8067 | 0.0704 |
| Probit 1 | test | 2763 | 249 | 270 | 50 | 0.5202 | 0.9822 | 0.0897 | 0.6658 | 0.9038 | 0.8075 | 0.0712 |
| Probit2 | test | 2758 | 253 | 266 | 55 | 0.5125 | 0.9804 | 0.0924 | 0.6569 | 0.9030 | 0.8061 | 0.0720 |
| NN1 | test | 2742 | 187 | 332 | 71 | 0.6397 | 0.9748 | 0.0774 | 0.6844 | 0.9129 | 0.8259 | 0.0650 |
| NN2 | test | 2740 | 197 | 322 | 73 | 0.6204 | 0.9740 | 0.0810 | 0.6851 | 0.9157 | 0.8314 | 0.0650 |

Portfolio with Macroeconomic Variable

Logit

The analysis is done on the same samples of portfolio, adding the macroeconomic indicator and the model is estimated on training sample with validation on test sample.

| [1] Likelihood Ratio | Test for Global Null Hyp | othesis: BETA=0 | Likeliho | Likelihood Ratio Test for Global Null Hypothesis: BETA=0 | | | | |
|--------------------------|--------------------------|-----------------|----------------|--|------------|---------------|--|--|
| | Likelihoo | d | | | Likelihood | | | |
| -2 Log Likeliho | ood Ratio | DF Pr > ChiSq | -2 | Log Likelihood | Ratio | DF Pr > ChiSq | | |
| Intercept Only Intercept | & Covariates Chi-Square | | Intercept Only | y Intercept & Covariates | Chi-Square | | | |
| 19352.26 | 10622.993 8729.26 | 64 51 <.0001 | 19352. | 26 10758.365 | 8593.8942 | 2 47 <.0001 | | |

| Analysis | Analysis of Maximum Likelihood Estimates –Logit (1) | | | | | | | Analysis of Maximum Likelihood Estimates | | | | |
|---------------|---|---------|----------|------------|------------|---------------|----|--|----------|------------|------------|--|
| | D | Estima | Standard | Wald | | Parameter | DI | F Estimate | Standard | Wald | Pr > ChiSq | |
| Parameter | F | te | Error | Chi-Square | Pr > ChiSq | | | | Error | Chi-Square | 2 | |
| Intercept | 1 | -3.6365 | 1.4412 | 6.3700 | 0.0116 | Intercept | 1 | -3.4977 | 1.3938 | 6.3 | 0.0121 | |
| Age | 1 | -0.0184 | 0.0044 | 17.8900 | <.0001 | Age | 1 | -0.0148 | 0.00422 | 12.3 | 0.0005 | |
| Expenses | 1 | 0.0018 | 0.0001 | 552.9500 | <.0001 | Expenses | 1 | 0.00175 | 7.4E-05 | 558.23 | <.0001 | |
| Income | 1 | -0.0007 | 0.0000 | 387.6800 | <.0001 | Income | 1 | -0.00075 | 3.8E-05 | 393.64 | <.0001 | |
| Interest_rate | 1 | 0.1146 | 0.0279 | 16.8800 | <.0001 | Interest_rate | 1 | 0.0298 | 0.018 | 2.73 | 0.0983 | |
| Loan Value | 1 | 0.0000 | 0.0000 | 27.7500 | <.0001 | loan_value | 1 | -2.26E-06 | 1.04E-06 | 4.74 | 0.0294 | |
| Payment | 1 | 0.0023 | 0.0001 | 250.6900 | <.0001 | Payment | 1 | 0.00198 | 0.00017 | 139.54 | <.0001 | |
| IMV_cust | 1 | 5.1807 | 0.3196 | 262.7200 | <.0001 | Term | 1 | -0.00004 | 1.5E-05 | 8.11 | 0.0044 | |

IMV_cust

5.2456

1

0.3172

273.46

<.0001

Portfolio with Macroeconomic Variable

Probit

| [1] Likeliho | od Ratio Test for Global | Null Hypoth | esis: BETA=0 |
|----------------|--------------------------|-------------|-----------------|
| | | Likelihood | |
| -2 Lo | og Likelihood | Ratio | DF $Pr > ChiSq$ |
| Intercept Only | Intercept & Covariates | Chi-Square | |
| 19352.20 | 5 10832.701 | 8519.5583 | 3 51<.0001 |

| [2] Likelihoo | d Ratio Test for | r Global N | Jull Hypoth | nesis: | BETA= | 0 |
|----------------|------------------|------------|-------------|--------|------------------|--------------|
| 21.0 | a Likelihood | | Likelihood | DE | $D_{\theta} > C$ | L :C~ |
| -2 LC | g Likennood | | Katio | DF | $Pr \ge C$ | nisq |
| Intercept Only | Intercept & Co | ovariates | Chi-Square | | | |
| 19352.20 | 5 1 | 0964.259 | 8388.0004 | 4 | 7<.0001 | |

| | Analysis of Maximum Likelihood Estimates | | | | | | | | | | | |
|---------------|--|-----------|------------|------------|------------|--|--|--|--|--|--|--|
| Parameter | DF I | Estimate | Standard | Wald | Pr > ChiSq | | | | | | | |
| | | | Error | Chi-Square | | | | | | | | |
| Intercept | 1 | -2.1725 | 5 0.7504 | 4 8.38 | 0.0038 | | | | | | | |
| Age | 1 | -0.00888 | 3 0.0022 | 5 15.59 | <.0001 | | | | | | | |
| Expenses | 1 | 0.000745 | 5 0.00003 | 1 564.52 | 2 <.0001 | | | | | | | |
| Income | 1 | -0.00033 | 3 0.00001 | 7 369.32 | 2 <.0001 | | | | | | | |
| Interest_rate | 1 | 0.0636 | 6 0.0148 | 8 18.58 | s <.0001 | | | | | | | |
| loan_value | 1 | -2.41E-06 | 6 4.32E-0 | 7 31.25 | .0001 | | | | | | | |
| Payment | 1 | 0.00108 | 3 0.000072 | 2 227.57 | <.0001 | | | | | | | |
| IMV_cust | 1 | 2.8377 | 0.1702 | 2 278.12 | 2 <.0001 | | | | | | | |

| Analysis of Maximum Likelihood Estimates | | | | | | | | | | | |
|--|----|-----------|----------|------------|------------|--|--|--|--|--|--|
| Parameter | DF | Estimate | Standard | Wald | Pr > ChiSq | | | | | | |
| | | | Error | Chi-Square | | | | | | | |
| Intercept | 1 | -2.0873 | 0.73 | 8.18 | 0.0042 | | | | | | |
| Age | 1 | -0.00684 | 0.00218 | 9.79 | 0.0018 | | | | | | |
| Expenses | 1 | 0.000749 | 3.1E-05 | 573.46 | <.0001 | | | | | | |
| Income | 1 | -0.00033 | 1.7E-05 | 382.87 | <.0001 | | | | | | |
| Interest_rate | 1 | 0.0157 | 0.00963 | 2.65 | 0.1034 | | | | | | |
| loan_value | 1 | -1.44E-06 | 5.27E-07 | 7.49 | 0.0062 | | | | | | |
| Payment | 1 | 0.000946 | 8.3E-05 | 130.31 | <.0001 | | | | | | |
| Term | 1 | -0.00002 | 8.02E-06 | 6.21 | 0.0127 | | | | | | |
| IMV_cust | 1 | 2.8475 | 0.1693 | 282.97 | <.0001 | | | | | | |

Portfolio with Macroeconomic Variable

Neural Networks

| Neural Networks | Tanh | Logit | ROC Curve |
|--|----------|----------|---|
| Train: Akaike's Information Criterion | 9381.67 | 9337.05 | Neural Networks with Macroeconomic Variable |
| Train: Schwarz's Bayesian Criterion | 10574.14 | 10529.53 | 10 |
| Train: Average Error Function | 0.19476 | 0.19381 | |
| Train: Error Function | 9085.67 | 9041.05 | |
| Train: Misclassification Rate | 0.07374 | 0.07117 | 0,8 |
| Train: Number of Wrong Classifications | 1720. | 1660 | |
| Valid: Average Error Function | 0.21533 | 0.21072 | 0.6 |
| Valid: Error Function | 2869.89 | 2808.47 | |
| Valid: Mean Squared Error | 0.06174 | 0.06047 | ensit |
| Valid: Misclassification Rate | 0.08013 | 0.07773 | [∞] 0,4 |
| Valid: Number of Wrong Classifications | 534 | 518 | |
| Test: Average Error Function | 0.21861 | 0.20920 | 0.2 |
| Test: Error Function | 1456.78 | 1394.12 | |
| Test: Mean of Squared Error | 0.06138 | 0.05939 | |
| Test: Misclassification Rate | 0.07713 | 0.07593 | 0,0 0,2 0,4 0,6 0,8 1,0 - NN-log with MV |
| Test: Number of Wrong Classifications | 257 | 253 | 1 - Specificity |

| | Macro | | | | | | | | | | | |
|----------|----------|------|--------|----------------------|------|-------------|-------------|----------|--------|--------|--------|-------------|
| | Result s | Cor | nfusio | n Mat <mark>r</mark> | ix | | | | | | | |
| Model | Sample | TN | FN | TP | FP | Sensitivity | Specificity | Misclass | KS | AUROC | AR | Brier Score |
| Logit1 | test | 2757 | 214 | 4 305 | 5 56 | 0.5877 | 0.9801 | 0.0810 | 0.6741 | 0.9084 | 0.8168 | 0.0666 |
| Logit 2 | test | 2757 | 222 | 1 298 | 8 56 | 0.5742 | 0.9801 | 0.0831 | 0.6700 | 0.9072 | 0.8144 | 0.0677 |
| Probit 1 | test | 2764 | - 235 | 5 284 | 4 49 | 0.5472 | 0.9826 | 0.0852 | 0.6671 | 0.9079 | 0.8159 | 0.0682 |
| Probit2 | test | 2765 | 230 | 6 283 | 3 48 | 0.5453 | 0.9829 | 0.0852 | 0.6664 | 0.9069 | 0.8138 | 0.0693 |
| NN1 | test | 2747 | 190 | 6 323 | 3 66 | 0.6224 | 0.9765 | 0.0786 | 0.7042 | 0.9201 | 0.8401 | 0.0615 |
| NN2 | test | 2754 | 182 | 1 338 | 8 59 | 0.6513 | 0.9790 | 0.0720 | 0.7037 | 0.9278 | 0.8556 | 0.0587 |

Model Improvement

•The results of regression logistic with macroeconomic variable incorporated are comparable with neural networks;



| Impro | ovement | | Confusi | on Matrix | trix Goodness of Fit | | | | | | | |
|----------|---------|-------|---------|-----------|----------------------|-------------|-------------|----------|-------|-------|-------|--------------------|
| Model | Sample | TN | FN | ТР | FP | Sensitivity | Specificity | Misclass | KS | AUROC | AR | Brier Score |
| Logit 2 | test | 0.22% | -3.49% | 2.76% | -9.68% | 2.76% | 0.22% | -4.81% | 1.40% | 0.43% | 0.96% | -3.72% |
| Logit1 | test | 0.07% | -4.46% | 3.39% | -3.45% | 3.39% | 0.07% | -4.26% | 0.03% | 0.47% | 1.04% | -4.01% |
| Probit 1 | test | 0.04% | -5.62% | 5.19% | -2.00% | 5.19% | 0.04% | -5.02% | 0.21% | 0.46% | 1.03% | -4.22% |
| Probit2 | test | 0.25% | -6.72% | 6.39% | -12.73% | 6.39% | 0.25% | -7.79% | 1.44% | 0.43% | 0.96% | -3.81% |
| NN1 | test | 0.18% | 4.81% | -2.71% | -7.04% | -2.71% | 0.18% | 1.55% | 2.88% | 0.78% | 1.73% | -5.39% |
| NN2 | test | 0.51% | -8.12% | 4.97% | -19.18% | 4.97% | 0.51% | -11.11% | 2.72% | 1.32% | 2.91% | -9.63% |

Model Improvement

•Detection accuracy of *bad* customers increases on average with 5.85% for probit regressions and with 3% for logistic regressions, neural networks instead recorded an increase of only 1.13%.;



Model Improvement

| Spiegelhalter Test | LOGIT1 | LOGIT2 | PROBIT1 | PROBIT2 | NN1 | NN2 |
|--------------------|--------|--------|---------|---------|--------|--------|
| Port | 0.7605 | 0.7330 | 0.1932 | 0.1773 | 0.8992 | 0.2235 |
| Macro | 0.7852 | 0.6458 | 0.1626 | 0.1133 | 0.2602 | 0.5743 |
| P-values | | | | | | |

•The Spiegelhalter Test indicates that, by accepting the null hypothesis on both portfolios with and without the macroeconomic variable, the observed default rates are close to the estimated probabilities of default

| | | Kuiper | | | | | | |
|----------|-----------|--------|----------|--|--|--|--|--|
| Model | Portfolio | Macro | | | | | | |
| Logit1 | 0.5 | 5478 | 0.567761 | | | | | |
| Logit 2 | 0.5 | 5367 | 0.554274 | | | | | |
| Probit 1 | 0.5 | 5025 | 0.529787 | | | | | |
| Probit2 | 0.4 | 930 | 0.528216 | | | | | |
| NN1 | 0.6 | 5145 | 0.598888 | | | | | |
| NN2 | 0.5 | 5945 | 0.630278 | | | | | |

•*Kuiper Score* is the difference between hit rate and false alarm rate and the grater the difference the better the classification between defaulters and non-defaulters

•The models that have the higher score are neural networks and from regressions class the stepwise logistic is the one that discriminates better.

Setting the optimal Cut-off

This issue of acceptance rate is a trade-off between the higher acceptance rate as profit generator and lower acceptance rate as loss in market share.

| Confusion Matrix | | | | | | | | |
|------------------|--------|------|----|------|-----|-------------|-------------|------------------|
| Model | Sample | TN F | ΝΊ | ΓP Ξ | FP | Sensitivity | Specificity | Misclass Rate |
| Logit1 | test | 2350 | 88 | 431 | 463 | 0.83044 | 0.83541 | 0.16537 |
| Logit 2 | test | 2327 | 91 | 428 | 486 | 0.82466 | 0.82723 | 0.17317 |
| Probit 1 | test | 2349 | 92 | 427 | 464 | 0.82274 | 0.83505 | 0.16687 |
| Probit2 | test | 2328 | 93 | 426 | 485 | 0.82081 | 0.82759 | 0.17347 |
| NN1 | test | 2391 | 85 | 434 | 422 | 0.83622 | 0.84998 | 0.15216 |
| NN2 | test | 2404 | 79 | 440 | 409 | 0.84778 | 0.85460 | 0.14646 |





Misclassification Cost

The model that minimizes the expected future loss is an optimal model of classification and considering the fact that there are two classes of customers, the future loss depends on the two types of misclassification errors.

| Cost comparison | | Confus | ion Matrix | | Goodness of Fit | | | | | |
|-----------------|--------|--------|------------|-----|-----------------|-------------|-------------|------------------|--------------------|---------|
| M odel | Sample | TN | FN | ТР | FP | Sensitivity | Specificity | Kuipers Score | Granger Pesaran | p-value |
| Logit1 | test | 2758 | 212 | 307 | 55 | 0.5915 | 0.9804 | 0.5720 | 38.47 | 0.000 |
| Logit 2 | test | 2755 | 216 | 303 | 58 | 0.5838 | 0.9794 | 0.5632 | 37.93 | 0.000 |
| Probit 1 | test | 2762 | 228 | 291 | 51 | 0.5607 | 0.9819 | 0.5426 | 37.42 | 0.000 |
| Probit2 | test | 2765 | 234 | 285 | 48 | 0.5491 | 0.9829 | 0.5321 | 37.13 | 0.000 |
| NN1 | test | 2741 | 186 | 333 | 72 | 0.6416 | 0.9744 | 0.6160 | 39.46 | 0.000 |
| NN2 | test | 2753 | 193 | 326 | 60 | 0.6281 | 0.9787 | 0.6068 | 39.69 | 0.000 |
| Logit1 | test | 2750 | 234 | 285 | 63 | 0.5491 | 0.9776 | 0.5267 | 36.05 | 0.000 |
| Logit 2 | test | 2755 | 216 | 303 | 58 | 0.5838 | 0.9794 | 0.5632 | 37.93 | 0.000 |
| Probit 1 | test | 2767 | 234 | 285 | 46 | 0.5491 | 0.9836 | 0.5328 | 37.28 | 0.000 |
| Probit2 | test | 2765 | 234 | 285 | 48 | 0.5491 | 0.9829 | 0.5321 | 37.13 | 0.000 |
| NN1 | test | 2740 | 186 | 333 | 73 | 0.6416 | 0.9740 | 0.6157 | 39.40 | 0.000 |
| NN2 | test | 2749 | 191 | 328 | 64 | 0.6320 | 0.9772 | 0.6092 | 39.58 | 0.000 |
| Logit1 | test | 2758 | 212 | 307 | 55 | 0.5915 | 0.9804 | 0.5720 | 38.47 | 0.000 |
| Logit 2 | test | 2755 | 216 | 303 | 58 | 0.5838 | 0.9794 | 0.5632 | 37.93 | 0.000 |
| Probit 1 | test | 2762 | 228 | 291 | 51 | 0.5607 | 0.9819 | 0.5426 | 37.42 | 0.000 |
| Probit2 | test | 2765 | 234 | 285 | 48 | 0.5491 | 0.9829 | 0.5321 | 37.13 | 0.000 |
| NN1 | test | 2744 | 184 | 335 | 69 | 0.6455 | 0.9755 | 0.6209 | 39.82 | 0.000 |
| NN2 | test | 2749 | 191 | 328 | 64 | 0.6320 | 0.9772 | 0.6092 | 39.58 | 0.000 |

Expected Loss = $P_B Cost_{Type \ I} Error Rate Type \ I + P_G Cost_{Type \ I} Error Rate Type \ II$

6.Stress Testing

• Scenario- income decreasing with 25% for public sector employers and increasing of Expenses with 4.5% for the whole portfolio

• This scenario impacts the average default probability with an increase of 1% on the public employers sector.



7.Conclusions

- Portfolio results concluded that neural networks have a higher accuracy than regressions;
- After including the macroeconomic variable, results showed that models like logistic regressions have accuracy as high as one of the neural network architectures.
- •Minimizing misclassification cost improves probit regressions by reducing the error of prediction with 8% and for logistic regressions and neural networks with 5%
- •The indicator of macroeconomic vulnerability could be part of a development model for credit risk based on a scorecard where the capacity of a client would be aligned to the macroeconomic conditions;

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Thank you!